

## 8.8 Factor by Grouping

\* If a polynomial has 4 terms, you can factor by grouping. (Not all expressions can be factored this way.)

\* Just like in 8.6, you look for common binomial factors.

First - group the 1<sup>st</sup> 2 terms & 2nd 2 terms  
Second - Factor GCF & look for a common binomial

Example 1:  $x^3 - 2x^2 + 3x - 6$   
 $(x^3 - 2x^2) + (3x - 6)$   
 $x^2(x - 2) + 3(x - 2)$

$$(x^2 + 3)(x - 2)$$

Example 2:  $b^3 + 8b^2 - 3b - 24$   
 $(b^3 + 8b^2) - (3b - 24)$   
 $b^2(b + 8) - 3(b + 8)$

$$(b^2 - 3)(b + 8)$$

\* (watch your signs)

\* Always check with FOIL

$$\begin{aligned}
 \text{Got it \#1 a)} \quad & 8t^3 + 14t^2 + 20t + 35 \\
 & (8t^3 + 14t^2) + (20t + 35) \\
 & 2t^2(4t+7) + 5(4t+7) \\
 & (2t^2+5)(4t+7)
 \end{aligned}$$

\* Always look for a GCF! st - Review Problem 2 on pg. 530

$$\begin{aligned}
 \text{* Got it \#2)} \quad & 6h^4 + 9h^3 + 12h^2 + 18h \\
 & 3h(2h^3 + 3h^2 + 4h + 6) \\
 & 3h(2h^3 + 3h^2) + (4h + 6) \\
 & 3h(h^2(2h+3) + 2(2h+3)) \\
 & \underline{3h(h^2+2)(2h+3)}
 \end{aligned}$$

\* Review Problem 3 on pg. 530

$$\begin{aligned}
 \text{* Got it 3?} \quad & 60x^3 + 34x^2 + 4x \\
 & 2(30x^2 + 17x + 2) \\
 & \text{Product of 60} \quad \left. \begin{array}{l} \\ \end{array} \right\} 12 \text{ \& } 5 \\
 & \text{Sum of 17} \quad \left. \begin{array}{l} \\ \end{array} \right\} 12 \text{ \& } 5
 \end{aligned}$$

$$\begin{aligned}
 & 2x(30x^2 + 12x + 5x + 2) \\
 & 2x(6x(5x+2) + 1(5x+2)) \\
 & \underline{2x(6x+1)(5x+2)}
 \end{aligned}$$

# 8-8 Practice

## Factoring by Grouping

Form G

Find the GCF of the first two terms and the GCF of the last two terms for each polynomial.

1.  $12x^3 + 3x^2 + 20x + 5$

2.  $6v^3 + 42v^2 + 5v + 35$

3.  $8t^3 + 36t^2 + 2t + 9$

4.  $10s^3 + 35s^2 + 6s + 21$

5.  $9m^3 - 6m^2 + 12m - 8$

6.  $8w^3 + 6w^2 - 28w - 21$

7.  $7r^3 + 16r^2 - 9r - 72$

8.  $21x^3 - 28x^2 - 6x + 8$

Factor each expression.

9.  $8j^3 + 4j^2 + 10j + 5$

10.  $2m^3 + 8m^2 + 9m + 36$

11.  $10s^3 + 25s^2 + 8s + 20$

12.  $6x^3 + 9x^2 + 2x + 3$

13.  $21x^3 + 6x^2 - 28x - 8$

14.  $8w^3 + 12w^2 + 10w + 15$

15.  $18r^3 - 12r^2 + 21r - 14$

16.  $36n^3 - 27n^2 - 8n + 6$

17.  $110b^3 + 77b^2 - 60b - 42$

18.  $64d^3 - 40d^2 - 24d + 15$

19.  $10s^3 + 80s^2 - 7s - 56$

20.  $25j^3 + 15j^2 - 5j - 3$

21.  $24c^3 - 84c^2 + 10c - 35$

22.  $27f^3 + 9f^2 - 24f - 8$

# 8-8 Practice (continued)

## Factoring by Grouping

Form G

Factor completely.

23.  $32x^3 + 8x^2 + 48x + 12$

24.  $45w^4 - 36w^3 + 15w^2 - 12w$

25.  $32k^4 - 16k^3 + 12k^2 - 6k$

26.  $6g^3 + 18g^2 + 60g + 180$

27.  $30b^4 - 45b^3 - 10b^2 + 15b$

28.  $32m^3 + 72m^2 - 80m - 180$

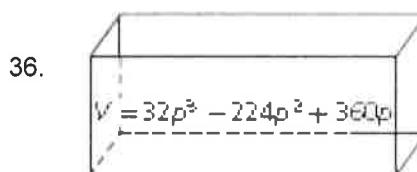
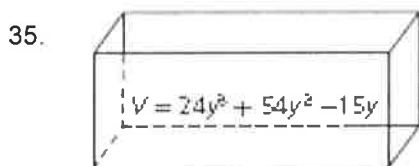
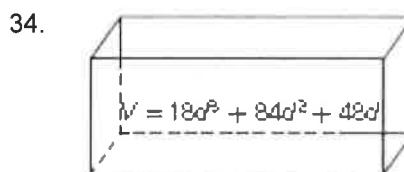
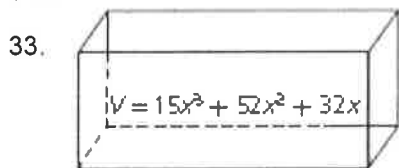
29.  $63j^4 + 84j^3 - 18j^2 - 24j$

30.  $96n^3 - 240n^2 - 168n + 420$

31.  $12e^4 + 18e^3 + 36e^2 + 54e$

32.  $60a^5 - 72a^4 - 210a^3 + 252a^2$

Find linear expressions for the possible dimensions of each rectangular prism.



37. A shipping box in the shape of a rectangular prism has a volume of  $12x^3 + 32x^2 + 20x$ . What linear expressions can represent possible dimensions of the box?

38. **Error Analysis** Describe and correct the error made in factoring completely.

~~$$16x^4 + 24x^3 + 64x^2 + 96x = 4x(4x^3 + 6x^2 + 16x + 24)$$

$$= 4x[2x^2(2x + 3) + 8(2x + 3)]$$

$$= 4x(2x^2 + 8)(2x + 3)$$~~

39. **Open-Ended** Write a 3-term expression for the volume of a rectangular prism that you can factor by grouping. Factor your polynomial.

Key

# 8-8

## Practice

Form G

### Factoring by Grouping

Find the GCF of the first two terms and the GCF of the last two terms for each polynomial.

1.  $12x^3 + 3x^2 + 20x + 5$

$3x^2, 5$

3.  $8t^3 + 36t^2 + 2t + 9$

$4t^2, 1$

5.  $9m^3 - 6m^2 + 12m - 8$

$3m^2, 4$

7.  $7r^3 + 16r^2 - 9r - 72$

$r^2, -9$

2.  $6v^3 + 42v^2 + 5v + 35$

$6v^2, 5$

4.  $10s^3 + 35s^2 + 6s + 21$

$5s^2, 3$

6.  $8w^3 + 6w^2 - 28w - 21$

$2w^2, -7$

8.  $21x^3 - 28x^2 - 6x + 8$

$7x^2, -2$

Factor each expression.

9.  $8j^3 + 4j^2 + 10j + 5$

$(4j^2 + 5)(2j + 1)$

11.  $10s^3 + 25s^2 + 8s + 20$

$(5s^2 + 4)(2s + 5)$

13.  $21x^3 + 6x^2 - 28x - 8$

$(3x^2 - 4)(7x + 2)$

15.  $18r^3 - 12r^2 + 21r - 14$

$(6r^2 + 7)(3r - 2)$

17.  $110b^3 + 77b^2 - 60b - 42$

$(11b^2 - 6)(10b + 7)$

19.  $10s^3 + 80s^2 - 7s - 56$

$(10s^2 - 7)(s + 8)$

21.  $24c^3 - 84c^2 + 10c - 35$

$(12c^2 + 5)(2c - 7)$

10.  $2m^3 + 8m^2 + 9m + 36$

$(2m^2 + 9)(m + 4)$

12.  $6x^3 + 9x^2 + 2x + 3$

$(3x^2 + 1)(2x + 3)$

14.  $8w^3 + 12w^2 + 10w + 15$

$(4w^2 + 5)(2w + 3)$

16.  $36n^3 - 27n^2 - 8n + 6$

$(9n^2 - 2)(4n - 3)$

18.  $64d^3 - 40d^2 - 24d + 15$

$(8d^2 - 3)(8d - 5)$

20.  $25j^3 + 15j^2 - 5j - 3$

$(5j^2 - 1)(5j + 3)$

22.  $27f^3 + 9f^2 - 24f - 8$

$(9f^2 - 8)(3f + 1)$

# 8-8

## Practice (continued)

Form G

### Factoring by Grouping

Factor completely.

23.  $32x^3 + 8x^2 + 48x + 12$   
 $4(2x^2 + 3)(4x + 1)$

25.  $32k^4 - 16k^3 + 12k^2 - 6k$   
 $2k(8k^2 + 3)(2k - 1)$

27.  $30b^4 - 45b^3 - 10b^2 + 15b$   
 $5b(3b^2 - 1)(2b - 3)$

29.  $63j^4 + 84j^3 - 18j^2 - 24j$   
 $3j(7j^2 - 2)(3j + 4)$

31.  $12e^4 + 18e^3 + 36e^2 + 54e$   
 $6e(e^2 + 3)(2e + 3)$

24.  $45w^4 - 36w^3 + 15w^2 - 12w$   
 $3w(3w^2 + 1)(5w - 4)$

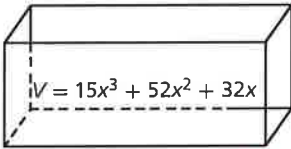
26.  $6g^3 + 18g^2 + 60g + 180$   
 $6(g^2 + 10)(g + 3)$

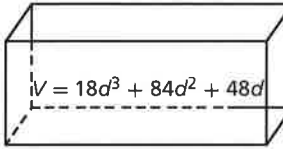
28.  $32m^3 + 72m^2 - 80m - 180$   
 $4(2m^2 - 5)(4m + 9)$

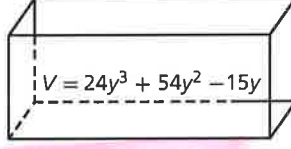
30.  $96n^3 - 240n^2 - 168n + 420$   
 $12(4n^2 - 7)(2n - 5)$

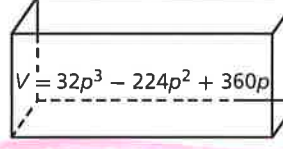
32.  $60a^5 - 72a^4 - 210a^3 + 252a^2$   
 $6a^2(2a^2 - 7)(5a - 6)$

Find linear expressions for the possible dimensions of each rectangular prism.

33.   
 $V = 15x^3 + 52x^2 + 32x$   
 $x, 5x + 4, 3x + 8$

34.   
 $V = 18d^3 + 84d^2 + 48d$   
 $6d, 3d + 2, d + 4$

35.   
 $V = 24y^3 + 54y^2 - 15y$   
 $3y, 4y - 1, 2y + 5$

36.   
 $V = 32p^3 - 224p^2 + 360p$   
 $8p, 2p - 5, 2p - 9$

37. A shipping box in the shape of a rectangular prism has a volume of  $12x^3 + 32x^2 + 20x$ . What linear expressions can represent possible dimensions of the box?  
 $4x, 3x + 5, x + 1$

38. **Error Analysis** Describe and correct the error made in factoring completely.

~~$$16x^4 + 24x^3 + 64x^2 + 96x = 4x(4x^3 + 6x^2 + 16x + 24)$$

$$= 4x[2x^2(2x + 3) + 8(2x + 3)]$$

$$= 4x(2x^2 + 8)(2x + 3)$$~~

In the first step, the GCF is  $8x$ , not  $4x$ .

39. **Open-Ended** Write a 3-term expression for the volume of a rectangular prism that you can factor by grouping. Factor your polynomial.

Answers may vary. Sample:  $x^5 + 4x^4 + 3x^3 = x^3(x + 3)(x + 1)$