

Chapter 3-6 Compound Inequalities

Part 1 (Solving & Graphing Compound Inequalities)

Compound Inequalities

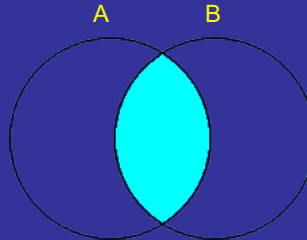
- Two simple inequalities joined by the word “and” or the word “or”.

What is the difference between

and and or?

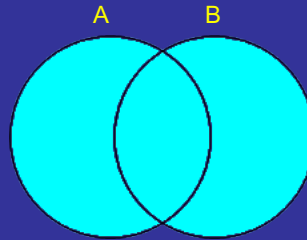
AND means
intersection

-what do the two items
have in common?



OR means union

-if it is in one item, it is in
the solution



Conjunction / “AND” Inequality

The solutions of two simple inequalities is where they **overlap** (The solution of one inequality **AND** the solution to the other inequality. The **INTERSECTION** of two solutions.)

$$x > -3 \text{ and } x \leq 1$$

$$-3 < x \leq 1$$

*Sometimes the word
“and” is not written,
but the “and” is
implied.

Conjunction / “AND” Inequality

$$-3 \leq x \leq 1$$

Read as:

- “x” is greater than or equal to -3 and less than or equal to 1
- “x” is in between -3 and 1, inclusive

***Inclusive means that both -3 & 1 are solutions*

Conjunction / “AND” Inequality

Solve

$$3 < 2m - 1 < 9$$

$$3 < 2m - 1 \text{ AND } 2m - 1 < 9$$

*The in between is SHARED.

Now Solve

Disjunction/ “OR” Inequality

The solution that makes one inequality true **OR** the other inequality true (The **UNION** of both solutions.)

$$-3p + 1 < -11 \quad \text{or} \quad p \leq -2$$



*The word “or”
MUST appear.

Now Solve

Graphing **Compound** Inequalities

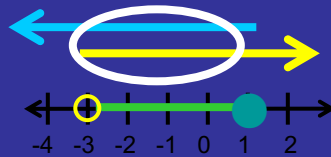
Steps:

- 1: Draw your line graph
- 2: Mark your answer with a open or closed circle
Open Circle: $<$ and $>$ symbols
Closed Circle: \leq and \geq symbols
- 3: Decide which direction your **arrows** should go to make the **inequalities** true
- 4: If “and”- Where do the lines (arrows) overlap?
If “or”- What are all the possible solutions?

Compound Inequalities

“and”

$$-3 < x \leq 1$$



Where do the lines overlap?

Conjunction / “AND” Inequality

The general rule is...

if the solutions do NOT contain an “overlap”, then there is **LIKELY** a mistake. (However, it is possible that the solution is an empty set.)

Compound Inequalities

Solve & Graph: $-3p + 1 < -11$ or $p \leq -2$

Solution: $p > 4$ or $p \leq -2$



What are all the possibilities?

Compound Inequalities

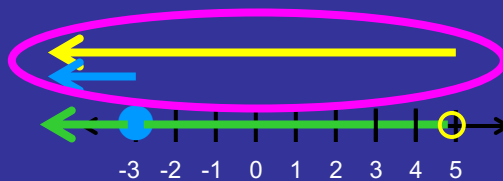
Solve and then graph

$$2y + 2 < 12$$

or

$$y - 3 \geq 2y$$

$$y < 5 \text{ or } -3 \geq y$$



What are all the possibilities?

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- Review Problem #1, 2, 3 & 4
- Got it? #1, 2, 3 & 4

Writing **Compound** Inequalities

Steps:

1: Determine directions of arrows

- If the arrows are **overlapping** then it is an **“and”** inequality.
- If the arrows are going in different directions (showing **all possible answer**) then it is an **“or”** inequality.

2: Mark your answers with a open or closed circle

Open Circle: $<$ and $>$ symbols

Closed Circle: \leq and \geq symbols

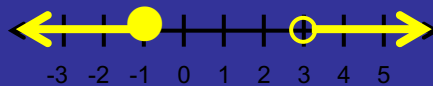
Examples: Writing Compound Inequalities



“and”

$$-2 \leq x \text{ and } x \leq 2$$

$$-2 \leq x \leq 2$$



“or”

$$x \leq -1 \text{ or } x > 3$$